



# From Skinner Box experiments to Black Box games

Radical behaviorism for experimental game theory

<https://osf.io/4n295/>

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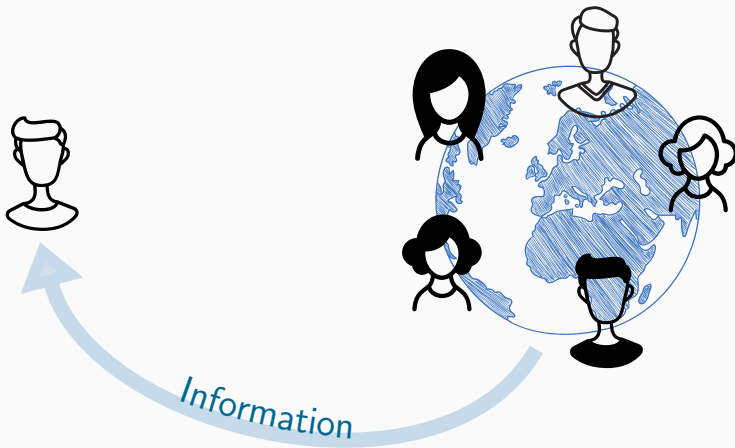
October 23, 2020

University of Zürich



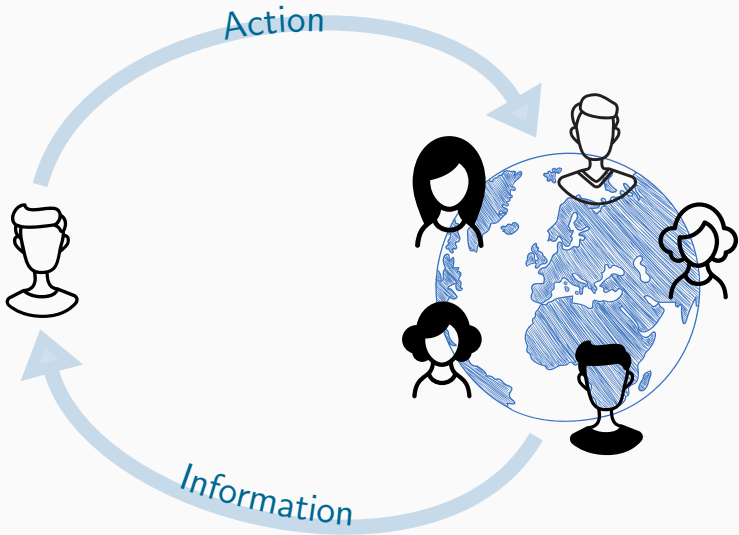
# Motivation

How useful are the existing explanations of learning in complex situations?



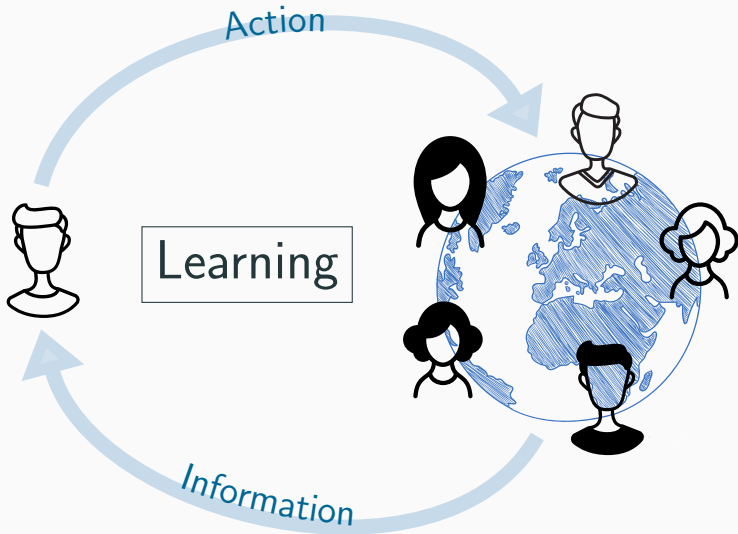
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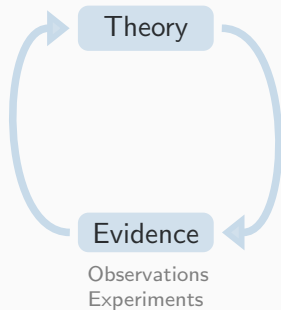
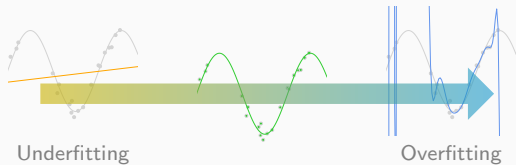


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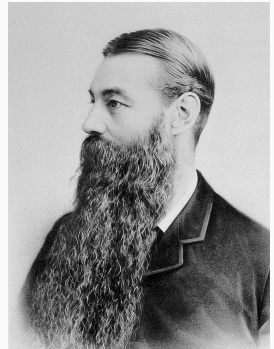
## Learning models



## Morgan's Canon

“ *In no case is an animal activity to be interpreted in terms of higher psychological processes, if it can be fairly interpreted in terms of processes which stand lower in the scale of psychological evolution and development.* ”

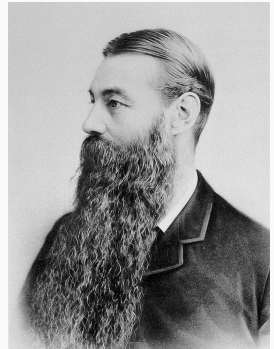
*C. Lloyd Morgan, 1903*



## Morgan's Canon

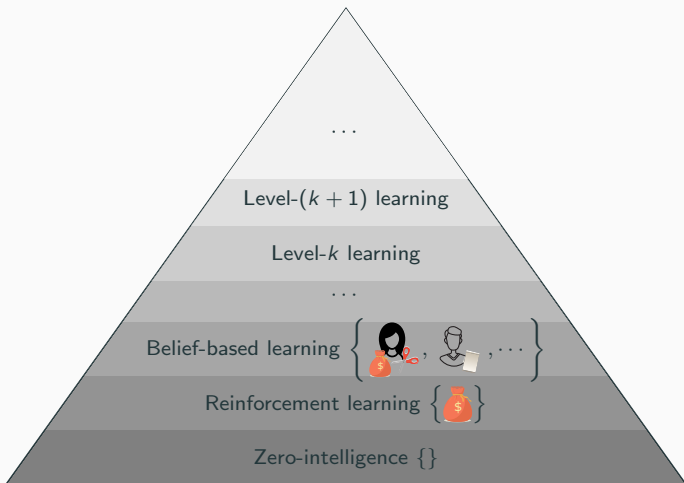
“ *In no case is [a human] activity to be interpreted in terms of higher psychological processes, if it can be fairly interpreted in terms of processes which stand lower in the scale of psychological evolution and development.* ”

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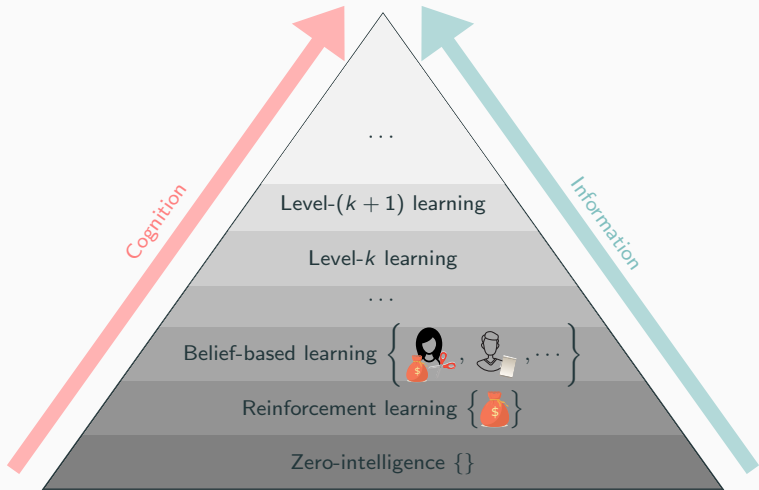




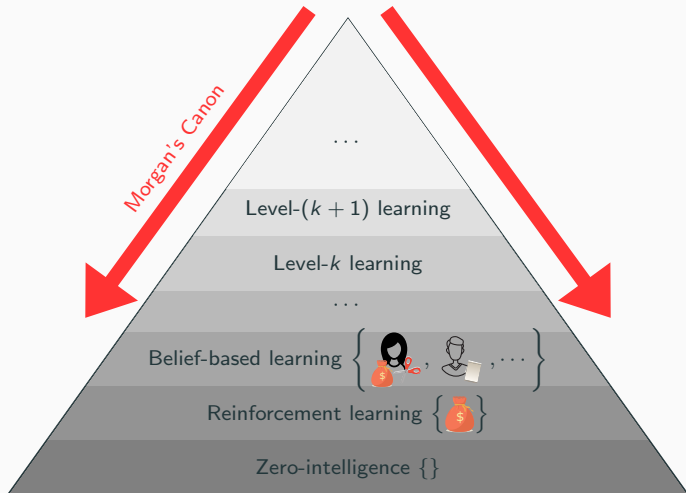
## Hierarchy of learning models



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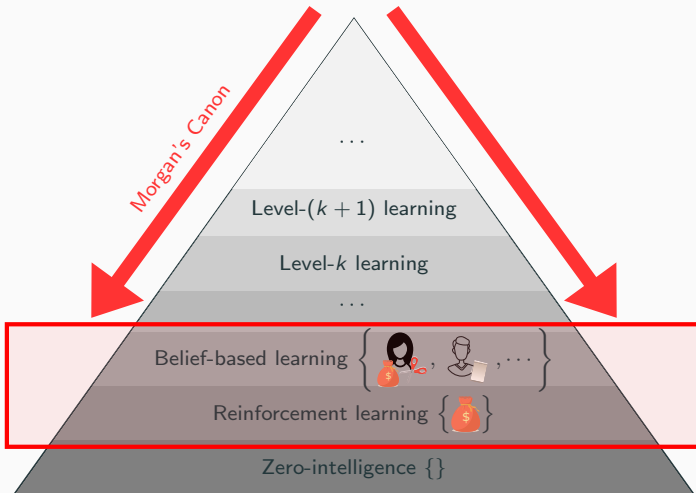


## Hierarchy of learning models



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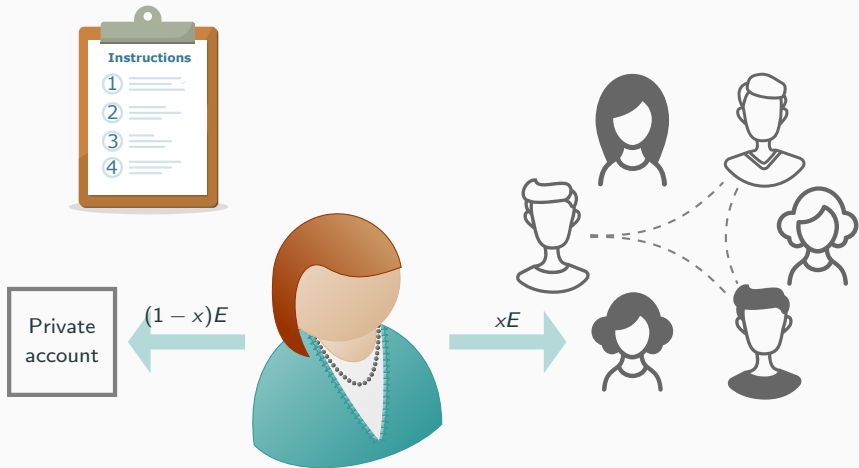
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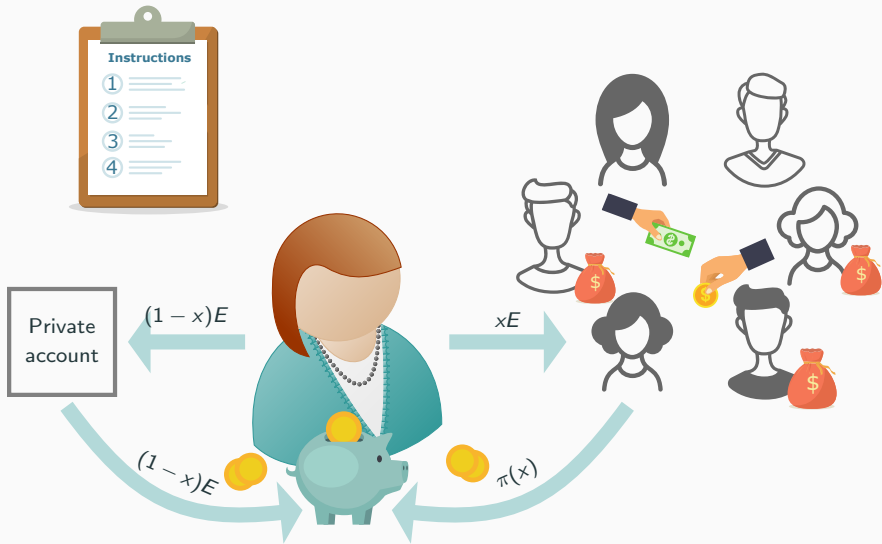
# Black Box approach



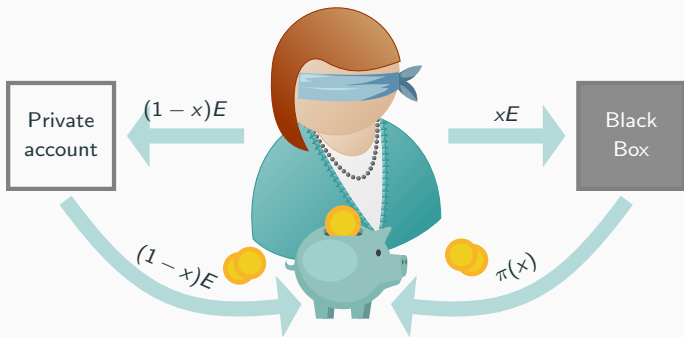
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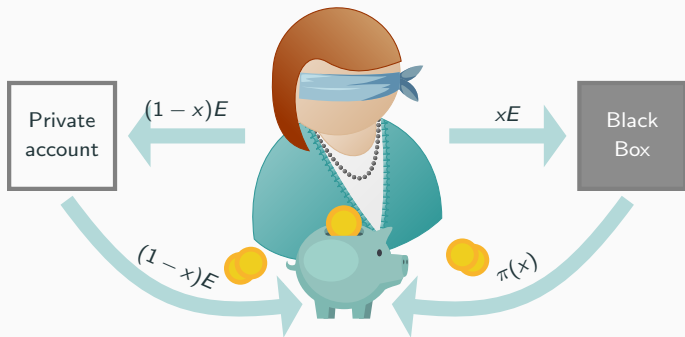
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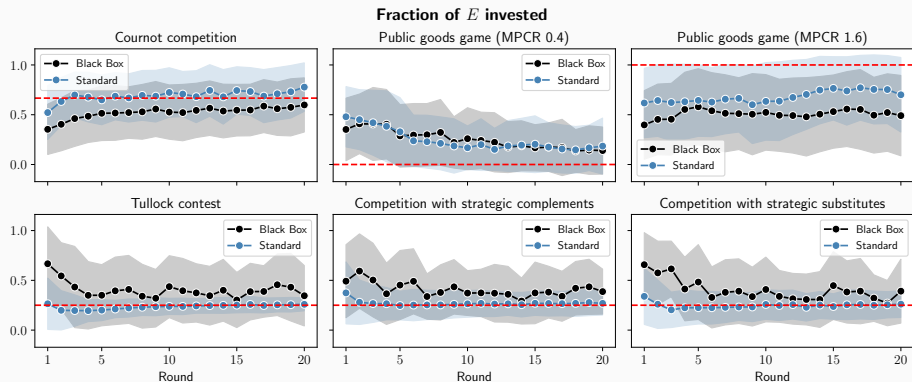


# Black Box approach

1. Learning model
2. Black Box  $\leftrightarrow$  standard game



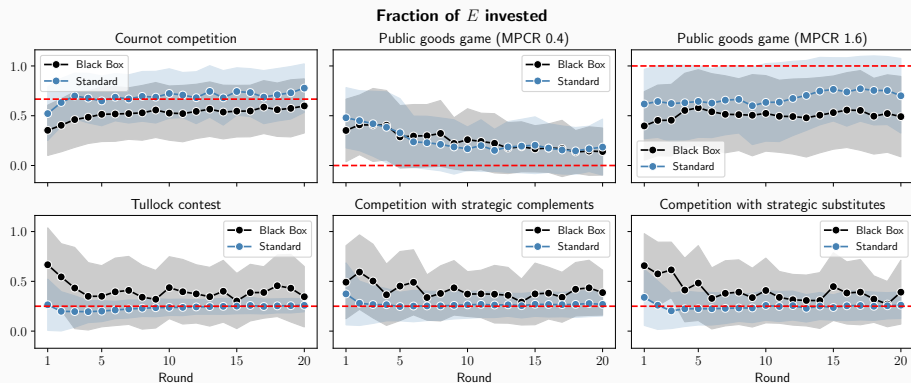
## 1. Experimental data



Setting	Sessions	Rounds	Subjects	Decisions
Black Box	24	20	391	7,820
Standard	32	20	580	11,600
<b>Total</b>	<b>56</b>	<b>20</b>	<b>971</b>	<b>19,420</b>

# Case study / Setup

## 1. Experimental data



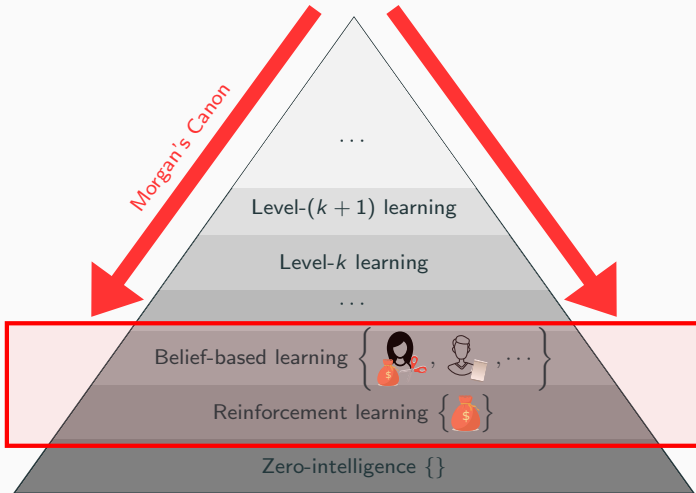
## 2. Learning model

Experience-weighted  
attraction learning

Reinforcement learning



Belief-based learning

## Hierarchy of learning models





# Case study / Results

Game	Parameter estimates				Goodness of fit				
	$\phi$	$\lambda$	$\delta$	$\rho$	LL	$\rho^2$	AIC	BIC	BS
Cournot	0.85	2.70	0.09	0.19	-8201	0.07	16411	16436	0.84
	0.84	6.90	0.35	0.32	-6094	0.06	12196	12220	0.80
PGG (MPCR 0.4)	0.82	4.55	0.52	0.37	-1864	0.11	3736	3756	0.65
	0.80	5.56	0.52	0.40	-1752	0.16	3512	3533	0.61
PGG (MPCR 1.6)	0.84	4.43	0.06	0.67	-2311	0.13	4629	4650	0.73
	0.82	9.55	0.46	0.75	-1454	0.22	2915	2935	0.56
Tullock	0.72	6.09	0.21	0.69	-840	0.16	1688	1705	0.71
	0.67	15.42	0.85	0.37	-2011	0.26	4029	4052	0.49
Complements	0.82	4.30	0.29	0.65	-933	0.10	1874	1891	0.79
	0.61	12.27	0.85	0.13	-2559	0.36	5125	5148	0.49
Substitutes	0.64	4.08	0.26	0.44	-842	0.18	1691	1708	0.70
	0.66	13.42	0.86	0.20	-2241	0.26	4491	4513	0.52

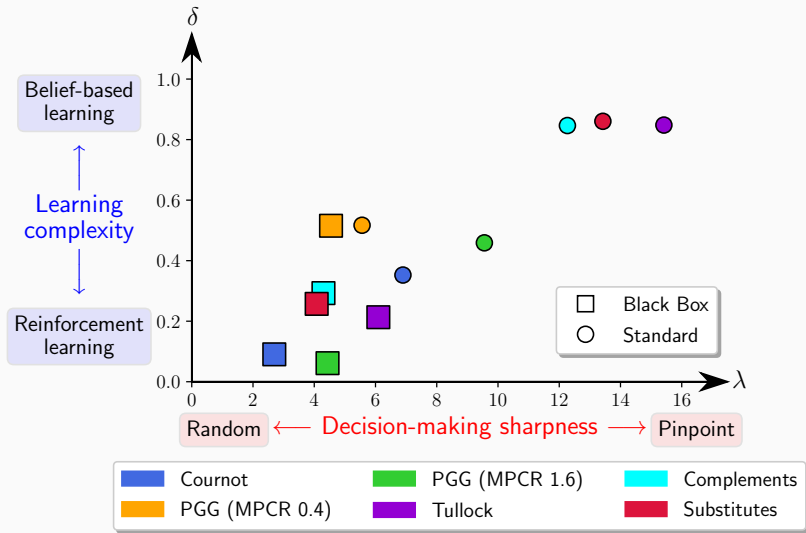
 Black Box  
 Standard

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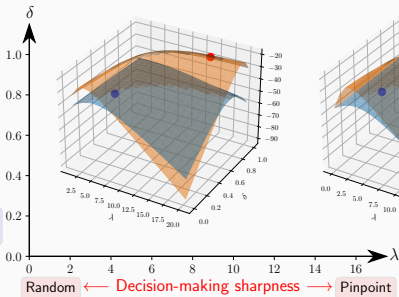
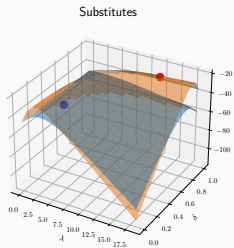
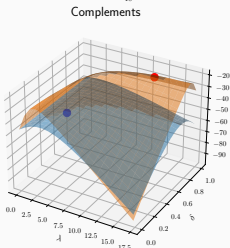
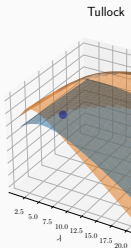
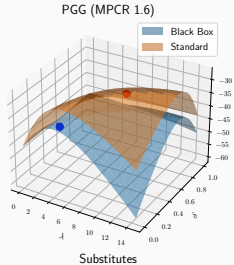
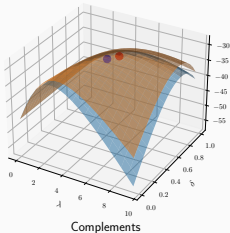
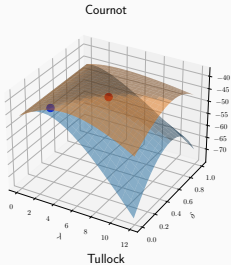
 Black Box  
 Standard

# Case study / Results



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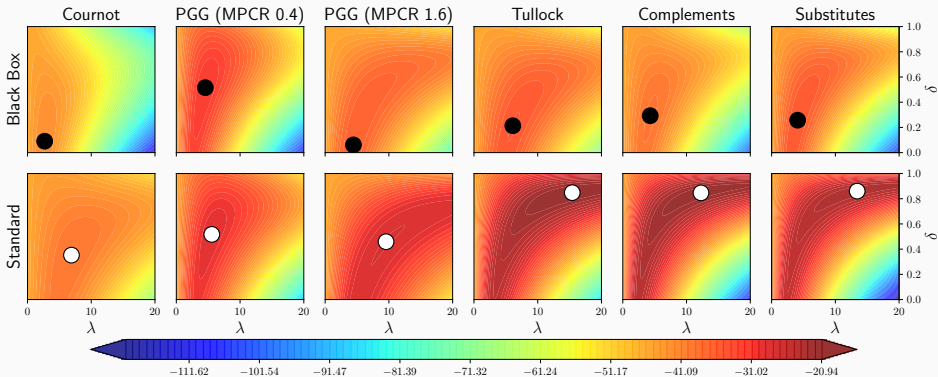
Log-likelihood over the  $(\lambda, \delta)$ -plane  
PGG (MPCR 0.4)





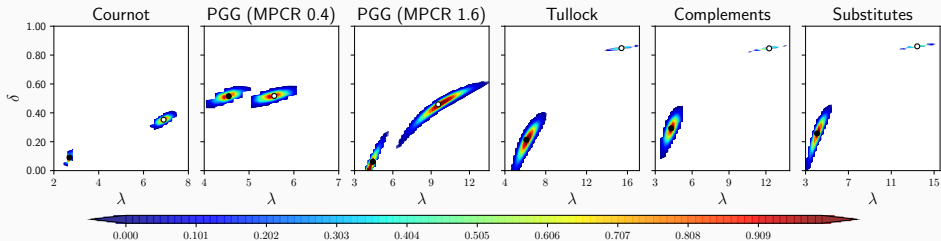
# Case study / Results

Log-likelihood over the  $(\lambda, \delta)$ -plane



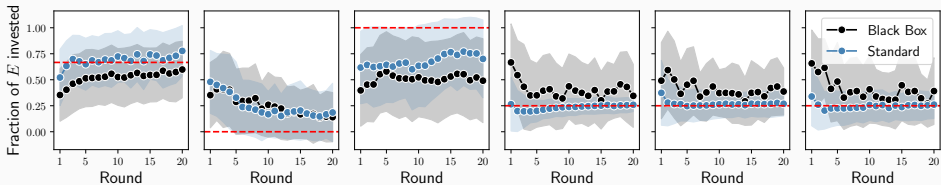
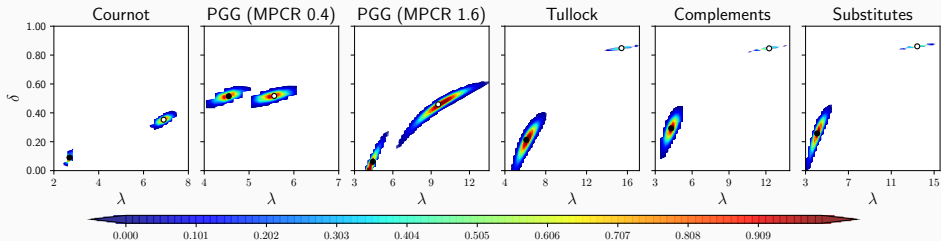
# Case study / Results

## $\chi^2$ likelihood-ratio test



# Case study / Results

## $\chi^2$ likelihood-ratio test



## Take-home message

*“ ... all models are approximations. Essentially, all models are wrong, but some are useful. However, the approximate nature of the model must always be borne in mind. ”*

*George E. P. Box & Norman R. Draper, 1987*